

Solubility & Complex-ion Equilibria

K_{sp}, molar solubility, the common-ion effect, Q vs K_{sp}, selective precipitation, and coupled equilibria.

01 K_{sp} expression

CORE RULE

K_{sp} = product of ion concentrations, each to its coefficient, in a saturated solution. The pure solid is excluded. $\text{AgCl} \rightleftharpoons \text{Ag}^+ + \text{Cl}^-$: $K_{\text{sp}} = [\text{Ag}^+][\text{Cl}^-]$.

02 K_{sp} in terms of solubility s

REFERENCE

Salt type	K _{sp}
MX	s^2
MX ₂ or M ₂ X	$4s^3$
MX ₃ or M ₃ X	$27s^4$
M ₂ X ₃	$108s^5$

03 Molar solubility from K_{sp}

METHOD

ICE with x for the reference ion, write the K_{sp} polynomial, solve for x. If solubility is given in g/L, convert to mol/L ($\div$ molar mass) before using K_{sp}.

04 Insoluble hydroxides & pH

CORE RULE

For $\text{M}(\text{OH})_n$, $[\text{OH}^-] = n \cdot s$, so $\text{pOH} = -\log[\text{OH}^-]$, $\text{pH} = 14 - \text{pOH}$. Given pH instead: $[\text{OH}^-] = 10^{-(14-\text{pH})}$, then solve K_{sp} for the metal-ion concentration.

05 Common-ion effect

CORE RULE

A shared ion already in solution goes into the ICE initial row, lowering molar solubility vs pure water. The x-small approximation ($x \ll$ common-ion concentration) is usually valid; check $x < 5\%$.

06 Q vs K_{sp} (will it precipitate?)

CORE RULE

Compute Q from initial ion concentrations (apply dilution when mixing: $[\text{ion}] \times V_{\text{part}}/V_{\text{total}}$). $Q < K_{\text{sp}} \rightarrow$ no precipitate; $Q > K_{\text{sp}} \rightarrow$ precipitates until $Q = K_{\text{sp}}$; $Q = K_{\text{sp}} \rightarrow$ just saturated.

07 Selective precipitation

CORE RULE

Find the counter-ion concentration each salt needs to hit $Q = K_{\text{sp}}$; the lowest threshold precipitates first. Comparing K_{sp} values directly is valid only for the same salt stoichiometry.

08 Complex-ion / coupled equilibria

CORE RULE

Coupling dissolution to complex formation raises solubility: $K_{\text{overall}} = K_{\text{sp}} \times K_{\text{f}}$. E.g. $\text{Al}(\text{OH})_3(\text{s}) + \text{OH}^- \rightleftharpoons \text{Al}(\text{OH})_4^-$. With excess ligand ($[\text{L}] \approx [\text{L}]_0$), a 1:1 salt gives $s = \sqrt{(K_{\text{overall}} \cdot [\text{L}])}$. Acid-coupled $\text{M}(\text{OH})_n$: $K = K_{\text{sp}}/K_{\text{w}}^n$.