

Colligative Properties

Van 't Hoff factor, freezing/boiling shifts, Raoult's law, osmotic pressure, and molar-mass back-calculation.

01 Van 't Hoff factor i

REFERENCE

Solute	i (predicted)
nonelectrolyte (glucose, urea)	1
NaCl, HCl, KBr	2
CaCl ₂ , Na ₂ SO ₄	3
AlCl ₃ , Na ₃ PO ₄	4
Al ₂ (SO ₄) ₃	5

i = particles per formula unit on full dissociation. Use the predicted (integer) i for forward calculations; measured i runs a bit lower at real concentrations (ion pairing).

02 Strong-electrolyte dissociation

CORE RULE

Each ion's concentration = compound concentration $\times$ its coefficient. Total dissolved particles = $i \times$ compound concentration. $\text{CaCl}_2 \rightarrow \text{Ca}^{2+} + 2\text{Cl}^-$ gives total = $3 \times [\text{CaCl}_2]$.

03 Freezing-point depression

CORE RULE

$\Delta T_f = K_f \cdot m \cdot i$ (m = molality). New FP = pure FP $- \Delta T_f$. For water (FP 0 °C) the depressed FP = $-\Delta T_f$. K_f is solvent-specific (supplied).

04 Boiling-point elevation

CORE RULE

$\Delta T_b = K_b \cdot m \cdot i$. New BP = pure BP $+ \Delta T_b$. For water (BP 100 °C) the elevated BP = $100 + \Delta T_b$. K_b is solvent-specific (supplied).

05 Common constants (°C·kg/mol)

REFERENCE

Solvent	K_f	K_b
water	1.86	0.512
benzene	5.12	2.53
chloroform	4.68	3.63
camphor	37.7	n/a

06 Raoult's law (vapor pressure)

CORE RULE

Nonvolatile solute: $\Delta P = X_{\text{solute}} \cdot P^\circ_{\text{solvent}}$, or $P_{\text{solution}} = X_{\text{solvent}} \cdot P^\circ_{\text{solvent}}$. Use particle-based mole fraction ($i \times n_{\text{solute}}$) for electrolytes. Two volatile components: $P_{\text{total}} = X_A \cdot P^\circ_A + X_B \cdot P^\circ_B$.

07 Osmotic pressure

CORE RULE

$\pi = i \cdot M \cdot R \cdot T$ with MOLARITY (not molality), $R = 0.0821 \text{ L} \cdot \text{atm}/(\text{mol} \cdot \text{K})$, T in K; π in atm. Given in molality/mass? You need density to convert to molarity.

08 Kelvin vs °C

WATCH OUT

Osmotic pressure needs T in Kelvin. But ΔT_f and ΔT_b are the same magnitude in °C or K, so apply K constants directly. Report final FP/BP in °C.

09 Molar mass from ΔT

METHOD

$n_{\text{solute}} = \Delta T / (K \cdot \text{kg}_{\text{solvent}} \cdot i)$, $K = K_f$ or K_b , $i = 1$ for a nonelectrolyte (the usual MW case). Then $\text{MW} = \text{mass}_{\text{solute}} / n_{\text{solute}}$.

10 Molar mass from osmotic pressure

METHOD

$n_{\text{solute}} = \pi \cdot V / (R \cdot T \cdot i)$, $i = 1$ for biomolecules (lysozyme, hemoglobin). Then $\text{MW} = \text{mass}_{\text{solute}} / n_{\text{solute}}$. π is often tiny, so convert torr/mmHg to atm first.

11 Molecular formula protocol

METHOD

Back-calc MW from ΔT or π ; get the empirical formula from % composition; $n = \text{MW} / \text{empirical-formula mass}$ (round to an integer); molecular formula = empirical $\times n$. Single-element (S_n): $n = \text{MW} / \text{atomic mass}$.